

2.8 Math 3C Review

1. Expand and simplify

$$\begin{aligned}\text{a) } (x-5)(x+3) \\ &= x^2 + 3x - 5x - 15 \\ &= x^2 - 2x - 15\end{aligned}$$

$$\begin{aligned}\text{b) } (x-4)^2 + 10 \\ &= (x-4)(x-4) + 10 \\ &= x^2 - 4x - 4x + 16 + 10 \\ &= x^2 - 8x + 26\end{aligned}$$

2. Factor the following

$$\begin{aligned}\text{a) } x^2 + 5x + 6 \\ &= (x+2)(x+3)\end{aligned}$$

$$\begin{aligned}\text{b) } x^2 + 3x - 18 \\ &= (x-3)(x+6)\end{aligned}$$

$$\begin{aligned}\text{c) } x^2 - 9x + 20 \\ &= (x-4)(x-5)\end{aligned}$$

$$\begin{aligned}\text{d) } x^2 + 2x - 48 \\ &= (x-6)(x+8)\end{aligned}$$

$$\begin{aligned}\text{e) } 2x^2 - 4x - 16 \\ &= 2(x^2 - 2x - 8) \\ &= 2(x+2)(x-4)\end{aligned}$$

$$\begin{aligned}\text{f) } 4x^2 + 12x + 8 \\ &= 4(x^2 + 3x + 2) \\ &= 4(x+1)(x+2)\end{aligned}$$

$$\begin{aligned}\text{g) } y = 4x^2 - 4x - 24 \\ &= 4(x^2 - x - 6) \\ &= 4(x+2)(x-3)\end{aligned}$$

$$\begin{aligned}\text{h) } y = 5x^2 + 5x - 30 \\ &= 5(x^2 + x - 6) \\ &= 5(x-2)(x+3)\end{aligned}$$

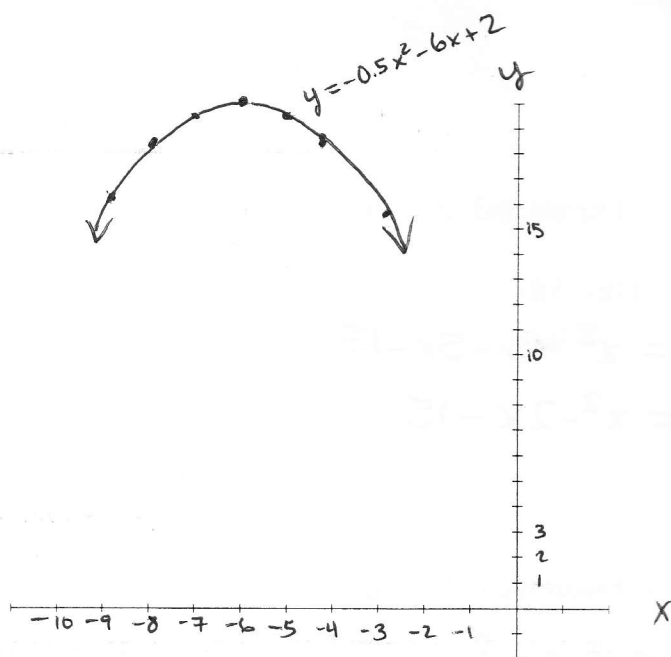
3. Change into standard form (expand):

$$\begin{aligned}\text{a) } y = -2(x+5)(x-3) \\ &= -2(x^2 - 3x + 5x - 15) \\ &= -2(x^2 + 2x - 15) \\ &= -2x^2 - 4x + 30\end{aligned}$$

$$\begin{aligned}\text{b) } y = 2(x+3)^2 + 5 \\ &= 2(x+3)(x+3) + 5 \\ &= 2(x^2 + 3x + 3x + 9) + 5 \\ &= 2x^2 + 6x + 6x + 18 + 5 \\ &= 2x^2 + 12x + 23\end{aligned}$$

2. Graph the parabola $y = -0.5x^2 - 6x + 2$

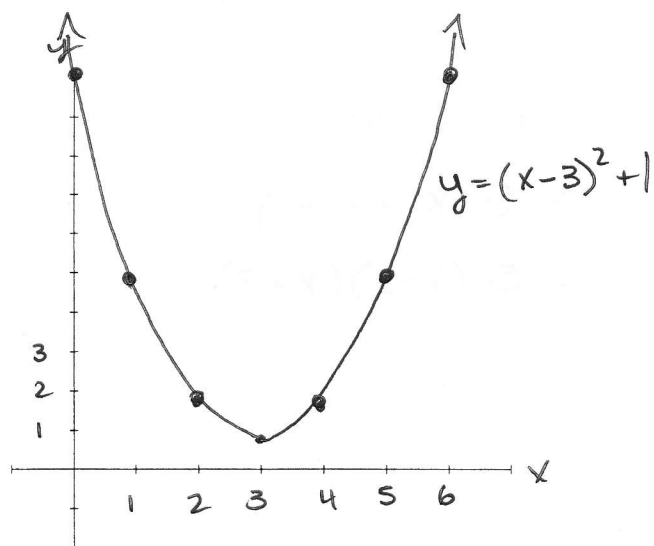
x	$y = -0.5x^2 - 6x + 2$	(x, y)
-9	$= -0.5(-9)^2 - 6(-9) + 2$	15.5
-8		18
-7		19.5
-6		20
-5		19.5
-4		18
-3		15.5



3. Graph the following without making a table of values

a) $y = (x-3)^2 + 1$

Vertex (3, 1)
Step pattern 1, 3, 5

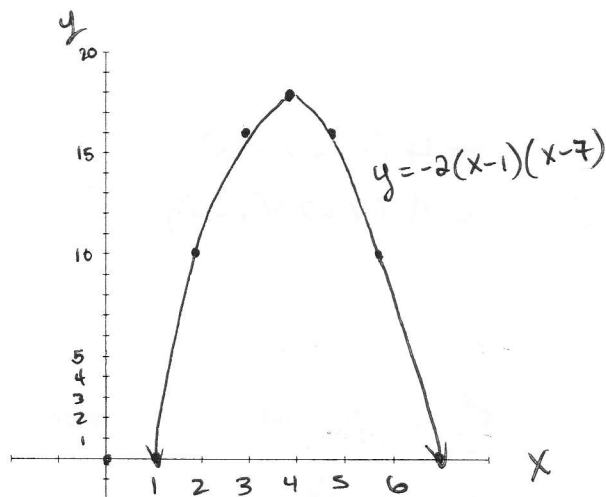


b) $y = -2(x-1)(x-7)$

Zeros: 1 & 7
axis of symmetry: $\frac{1+7}{2}$
 $x = 4$

Vertex (4, 18)
Step pattern -2, -6, -10

Sub $x=4$ into equation
 $= -2(4-1)(4-7)$
 $= -2(3)(-3)$
 $= 18$



c) $y = x^2 - 8x + 15$

$$y = (x-3)(x-5)$$

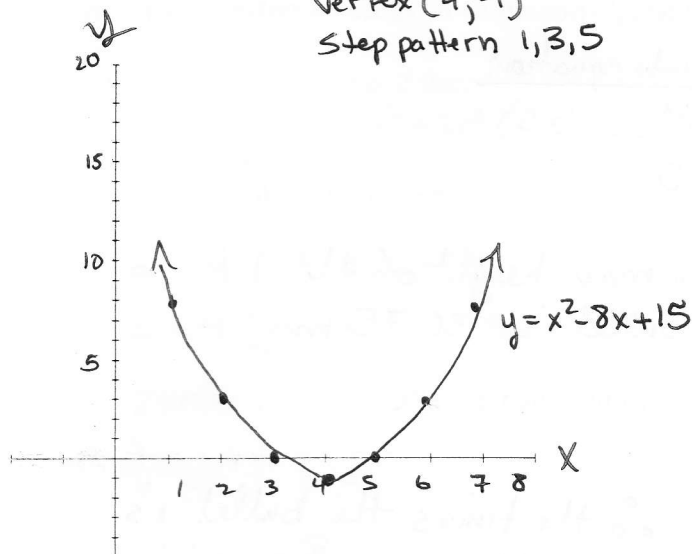
zeros 3, 5
Axis of symm: $\frac{3+5}{2}$

$$x = 4$$

Vertex (4, -1)

Step pattern 1, 3, 5

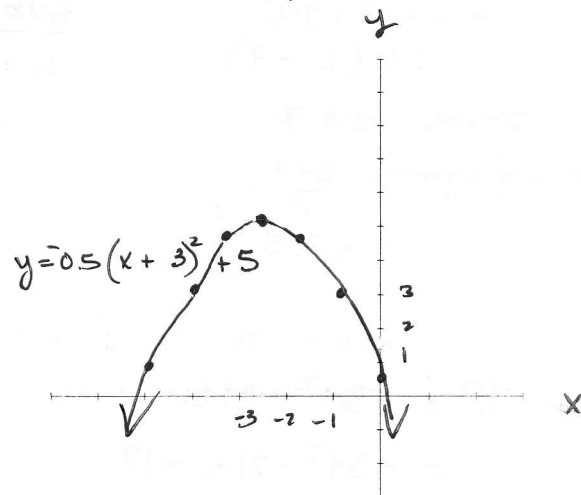
$$\begin{aligned} \text{Sub } x &= 4 \\ y &= (4-3)(4-5) \\ &= (1)(-1) \\ &= -1 \end{aligned}$$



d) $y = -0.5(x+3)^2 + 5$

Vertex (-3, 5)

Step pattern: -0.5, -1.5, -2.5



4. Change to factored form

a) $y = x^2 - 5x - 24$

$$= (x+3)(x-8)$$

b) $y = -3x^2 + 15x + 18$

$$\begin{aligned} &= -3(x^2 - 5x - 6) \\ &= -3(x+1)(x-6) \end{aligned}$$

c) $h = 6x^2 + 36x$

$$= 6x(x+6)$$

d) $h = 2t^2 + 2t - 24$

$$= 2(t^2 + t - 12)$$

$$= 2(t-3)(t+4)$$

e) $y = -7x^2 - 21x$

$$= -7x(x+3)$$

f) $h = -7t^2 + 21t$

$$= -7t(t-3)$$

5. A rifle is fired from a hole in the ground, at an angle into the air. The height, h , of the bullet is given by

$$h = -3t^2 + 21t$$

- a) What is the maximum height of the bullet?

$$= -3t^2 + 21t$$

$$= -3t(t - 7)$$

$$\text{Zeros: } 0 \text{ \& } 7$$

$$\text{axis of symm: } \frac{0+7}{2}$$

$$x = 3.5$$

Sub $x = 3.5$ into equation

$$h = -3(3.5)^2 + 21(3.5)$$

$$= 36.75$$

\therefore the max height of the bullet is 36.75 m

- b) At what times is the bullet exactly 18 m in the air (hint: when $h = 18$)?

$$18 = -3t^2 + 21t$$

$$= -3t^2 + 21t - 18$$

$$= -3(t^2 - 7t + 6)$$

$$= -3(t - 1)(t - 6)$$

$$\text{Zeros: } 1 \text{ \& } 6$$

\therefore the times the bullet is exactly 18 m in the air is 1 & 6 seconds.

- c) When is the bullet at ground level (hint: when $h = 0$)?

The bullet is at ground level at 7 seconds.

- d) Put the equation in vertex form

$$y = a(x - h)^2 + k$$

$$= -3(x - 3.5)^2 + 36.75$$

6. The Profit, P , earned by making coffee mugs is given by $P = -4n^2 + 64n - 60$ where
“ n is the number of mugs in thousands”, and “ P is the profit in thousands of dollars.”

a) What is the profit/loss if they sell zero mugs? $n=0$

$$P = -4(0)^2 + 64(0) - 60$$

$$P = -60$$

∴ if zero mugs are sold
they lose \$18 000.

b) What is the maximum profit?

$$= -4(n^2 - 16n + 15)$$

$$= -4(n-1)(n-15)$$

$$\text{Zeros: } 1 \text{ \& } 15$$

$$\text{Axis of sym: } \frac{1+15}{2}$$

$$x = 8$$

sub $x=8$ into equation

$$= -4(8)^2 + 64(8) - 60$$

$$= 196$$

∴ the max profit is \$196 000.

c) How much profit do they make if they sell 8000 mugs?

$$= -4(8)^2 + 64(8) - 60$$

$$= 196$$

∴ they make \$196 000 in profit if they
sell 8000 mugs.

d) How many mugs must they sell to make \$ 180,000 profit?

$$180 = -4n^2 + 64n - 60$$

$$= -4n^2 + 64n - 60 - 180$$

$$= -4n^2 + 64n - 240$$

$$= -4(n^2 - 16n + 60)$$

$$= -4(n-6)(n-10)$$

∴ they have to make
6000 or 10 000 mugs
to make \$180 000
in profit.